

1 Use the trapezium rule with n intervals of equal width to estimate the value of each integral.

a
$$\int_{1}^{5} x \ln(x+1) dx$$

$$n = 2$$

$$\mathbf{b} \quad \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \cot x \, \, \mathrm{d}x$$

$$n = 2$$

$$\mathbf{c} = \int_{-2}^{2} e^{\frac{x^2}{10}} dx$$

$$n = 4$$

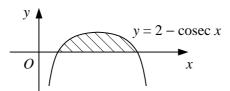
a
$$\int_{1}^{5} x \ln(x+1) dx$$
 $n=2$ **b** $\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \cot x dx$ $n=2$ **c** $\int_{-2}^{2} e^{\frac{x^{2}}{10}} dx$ $n=4$ **d** $\int_{0}^{1} \arccos(x^{2}-1) dx$ $n=4$ **e** $\int_{0}^{0.5} \sec^{2}(2x-1) dx$ $n=5$ **f** $\int_{0}^{6} x^{3}e^{-x} dx$ $n=6$

$$e \int_0^{0.5} \sec^2{(2x-1)} dx$$
 $n =$

$$\mathbf{f} = \int_{0}^{6} x^{3} e^{-x} dx$$

$$n = 6$$

2



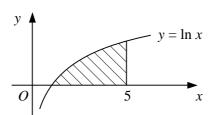
The diagram shows the curve with equation $y = 2 - \csc x$, $0 < x < \pi$.

- **a** Find the exact x-coordinates of the points where the curve crosses the x-axis.
- **b** Use the trapezium rule with four intervals of equal width to estimate the area of the shaded region bounded by the curve and the *x*-axis.

 $f(x) \equiv \frac{\pi}{6} + \arcsin(\frac{1}{2}x), x \in \mathbb{R}, -2 \le x \le 2.$ 3

- **a** Use the trapezium rule with three strips to estimate the value of the integral $I = \int_{-1}^{2} f(x) dx$.
- **b** Use the trapezium rule with six strips to find an improved estimate for *I*.

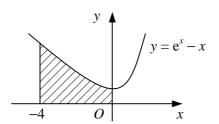
4



The shaded region in the diagram is bounded by the curve $y = \ln x$, the x-axis and the line x = 5.

- a Estimate the area of the shaded region to 3 decimal places using the trapezium rule with
 - i 2 strips
- ii 4 strips
- iii 8 strips
- **b** By considering your answers to part **a**, suggest a more accurate value for the area of the shaded region correct to 3 decimal places.
- **c** Use integration to find the true value of the area correct to 3 decimal places.

5



The shaded region in the diagram is bounded by the curve $y = e^x - x$, the coordinate axes and the line x = -4. Use the trapezium rule with five equally-spaced ordinates to estimate the volume of the solid formed when the shaded region is rotated completely about the x-axis.